

Name: Mr. Konichek Quiz 2: Ch 3.1 – 3.3

Draw a box around your final answers. No partial credit will be given.

- 3.1
#17
1. Find the derivative of the function: $f(x) = 5x^2 - 3x + 7$

$$f'(x) = 10x - 3$$

- 3.1
#13
2. Find the derivative of the function: $f(x) = 3\sqrt{x} = 3(x^{1/2})$

$$f'(x) = \frac{3}{2} x^{-1/2} = \boxed{\frac{3}{2\sqrt{x}}}$$

3. Let $f(x) = 2x^3 - 4x$. Find $f'(-2)$.

3.1
#35

$$f'(x) = 6x^2 - 4$$

$$f'(-2) = 6(-2)^2 - 4 = 24 - 4 = \boxed{20}$$

- 3.1
#29
4. Find the derivative of the function: $f(t) = \frac{4}{t^4} - \frac{3}{t^3} + \frac{2}{t} = 4t^{-4} - 3t^{-3} + 2t^{-1}$

final answer

$$\frac{-2t^3 + 9t^{-4} - 16}{t^5}$$

$$f'(t) = -16t^{-5} + 9t^{-4} - 2t^{-2}$$
$$f'(t) = \frac{-16}{t^5} + \frac{9}{t^4} - \frac{2}{t^2} = \frac{-16 + 9t^{-2} - 2t^3}{t^5}$$

- 3.2
#1
5. Find the derivative of the function: $f(x) = 2x(x^2 + 1)$ [2 lines]

$$f'(x) = 2x(2x) + (x^2 + 1)(2)$$
$$= 4x^2 + 2x^2 + 2$$
$$= \boxed{6x^2 + 2}$$

6. Find the derivative of the function: $f(x) = (3x+1)(x^2 - 2)$ [2 lines]

3.2 #5

$$\begin{aligned} f'(x) &= (x^2 - 2)(3) + (3x+1)(2x) \\ &= 3x^2 - 6 + 6x^2 + 2x \\ &= \boxed{9x^2 + 2x - 6} \end{aligned}$$

7. Find the derivative of the function: $f(s) = \frac{s^2 - 4}{s+1}$ [2 lines]

3.2 #21

$$\begin{aligned} f'(s) &= \frac{(s+1)(2s) - (s^2 + s)(1)}{(s+1)^2} \\ f'(s) &= \boxed{\frac{s^2 + 2s - s}{(s+1)^2}} \end{aligned}$$

8. Find the derivative of the function: $f(x) = (2x-1)^3$ [2 lines]

3.3 #1

$$\begin{aligned} f'(x) &= 3(2x-1)^2(2) \\ f'(x) &= \boxed{6(2x-1)^2} \end{aligned}$$

9. Find the derivative of the function: $f(x) = (x^2 + 1)^3 - (x^3 + 1)^2$ [2 lines]

3.3 #23

$$\begin{aligned} f'(x) &= 3(x^2 + 1)^2(2x) - 2(x^3 + 1)(3x^2) \\ f'(x) &= \boxed{6x(x^2 + 1)^2 - 6x^2(x^3 + 1)} \quad \text{OR} \quad 6x \left[(x^2 + 1)^2 - x(x^3 + 1) \right] \\ \text{final answer } f'(x) &= \boxed{6x(2x^2 - x + 1)} \end{aligned}$$

10. Find the derivative of the function: $f(x) = \left(\frac{x+3}{x-2} \right)^{-5}$ [2 lines]

3.3 #33

$$\begin{aligned} f'(x) &= 3 \left(\frac{(x+3)}{(x-2)} \right)^2 \frac{(x-2)(1)^2 - (x+3)(1)}{(x-2)^2} \\ &= \boxed{-15 \frac{(x+3)^2}{(x-2)^4}} \end{aligned}$$