The following rules apply:

- 1. All questions are worth either 1 point or no points at all. In other words, there is no partial credit so check your solutions carefully.
- 2. This assignment can replace your lowest un-dropped quiz score.
- 3. You can consult with ANY person or group of persons with the exception of me or any member of my immediate family.
- 4. The assignment must be done on <u>a separate sheet</u> in your own handwriting. No typed/PDF/emailed solutions.
- 5. STAPLE this coversheet to the front of your solutions. Do not write on it.
- 6. Note the due date above. The "due time" is as soon as you walk through the door.
- 7. I do not give solutions/corrections for the extra credit. So I suggest handing it in early so you will have time to make corrections and resubmit. If you resubmit, please include all previously graded versions so I can update your score.

Sketch the following curves. Include the extrema and inflection points, if any.

- 1. f'(x) and f''(x) are always positive.
- **2.** f'(x) is always negative and f''(x) is always positive.
- 3. f'(x) and f''(x) are always negative.
- **4.** f'(x) is always positive and f''(x) is always negative.

$$f(0) = 2, f(1) = 0, f(2) = -2, f'(0) = 0, f'(2) = 0,$$
5. $f'(x) > 0$ on $(-\infty, 0) \cup (2, \infty)$, $f'(x) < 0$ on $(0, 2)$
 $f''(1) = 0$, $f''(x) > 0$ on $(1, \infty)$, $f''(x) < 0$ on $(-\infty, 1)$

$$f(-2) = -2, f(0) = 1, f(2) = 4, f'(-2) = 0, f'(2) = 0,$$
6. $f'(x) > 0$ on $(-2, 2), f'(x) < 0$ on $(-\infty, -2) \cup (2, \infty)$
 $f''(0) = 0, f''(x) > 0$ on $(-\infty, 0), f''(x) < 0$ on $(0, \infty)$

7.
$$f(2) = 3, f(4) = 5, f(6) = 7, f'(2) = 0, f'(6) = 0,$$

 $f''(x) > 0 \text{ on } (-\infty, 4), f''(x) < 0 \text{ on } (4, \infty), f''(4) = 0$

8.
$$f(0) = 1, f(2) = -3, f(1) = -1, f'(0) = 0, f'(2) = 0,$$

 $f'(x) > 0 \text{ on } (-\infty, 0) \cup (2, \infty), f'(x) < 0 \text{ on } (0, 2)$
 $f''(1) = 0, f''(x) > 0 \text{ on } (1, \infty), f''(x) < 0 \text{ on } (-\infty, 1)$

$$f'(0) = f'(2) = f'(4) = 0,$$
9. $f'(x) > 0$ on $(-\infty, 0) \cup (2, 4)$, $f'(x) < 0$ on $(0, 2) \cup (4, \infty)$
 $f''(x) > 0$ on $(1, 3)$, $f''(x) < 0$ on $(-\infty, 1) \cup (3, \infty)$

$$f(0) = -2, f(1) = 0, f(2) = 4,$$
10.
$$f'(0) = 0, f'(2) = 0, f'(1) = undefined$$

$$f'(x) > 0 \ on(0,1) \cup (1,2), f'(x) < 0 \ on(-\infty,0) \cup (2,\infty)$$

$$f''(1) = undefined, f''(x) > 0 \ on(-\infty,1), f''(x) < 0 \ on(1,\infty)$$